Stress Free Stats Regression Warnings

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- Model mis-specification
- Diagnostics
- Measurement error
- Remedies
- Influential data points
- Diagnostics
- Remedies

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- As mentioned, mis-specifying your model is the gravest mistake you can committ
- Missing relevant predictors should be added to the model in order to capture the true relationships.
- WE MUST RELY ON THEORY to know what is missing!
- But our theories are often too general
- Since we do not know what is missing, we put in everything
- This is very bad: overspecifying the model -> collinearity and inflated standard errors
- Can show relationships which are just random (not causal)

True:
$$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \epsilon_i$$

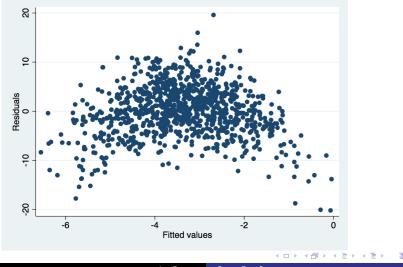
Estimated: $y_i = \beta_0 + \beta_1 x_i + \epsilon_i$

- Parameter estimates will be *biased* and *inconsistent* and standard errors may also be biased.
- Selecting a wrong functional form is like omitting a relevant predictor, which produces bias.
- The omission of z from the estimated model biases the estimate of $\hat{\beta}_1$ in the following way:

$$\hat{\beta_1} = \beta_1 + \beta_2 \frac{Cov[x,z]}{Var[x]}$$
if $\beta_2 > 0$ and $Cov[x,z] > 0$ then positive bias
if $\beta_2 < 0$ and $Cov[x,z] > 0$ then negative bias
if $\beta_2 < 0$ and $Cov[x,z] < 0$ then positive bias
if $\beta_2 > 0$ and $Cov[x,z] < 0$ then positive bias

Incorrect Functional Form 2

True: $y_i = \beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \beta_3 r_i + \beta_4 z_i + \epsilon_i$ Estimated: $y_i = \beta_0 + \beta_1 x_i + \epsilon_i$



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- Basic logic is: if there is some systematic shift in residuals versus fitted values of our model, this model is misspecified.
- We can try to find predictors that can explain the residual variation these predictors are the missing variables of the original model
- Plot residuals versus fitted values and look for an even band. If the band is curved, that suggests a missing quadratic term etc.
- R: plot(model\$residuals, model\$fitted)

Measurement Error

• Implicit assumption of OLS: no measurement error. In reality, error exists.

• Random error on Y

• The estimator will be *unbiased* since the randomness of error means that its mean remains =0. But *standard errors will be inflated* since error increases the estimator variance

Systematic error on Y

• Causes a bias in the intercept coefficient, but not in the slopes. It 'shifts' the function along the y axis.

Random error on X

- Error on X: values of X are correlated with the error term.
- We get biased and inconsistent estimates of the coefficient.
- The effect of the predictor with error is underestimated, which is called *attenuation bias*.

- Instrumental Variables
 - Find a variable that is correlated with X but not with ϵ .
 - This is not a 'proxy', which is a variable used to measure latent
 - or unmeasurable, unobservable variables.
- Structural Equations
 - A matter for another class

SQA

- Outliers and influential data that is observations that 'stick out' – can significantly alter our statistical results.
- Outlier is an atypical value on y,
- Leverage value is an atypical value on x,
- Influential value is an atypical value in both x and y

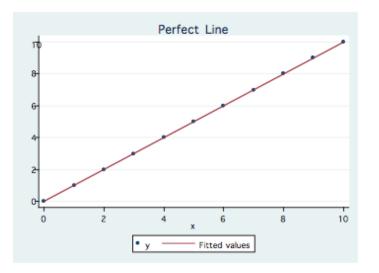


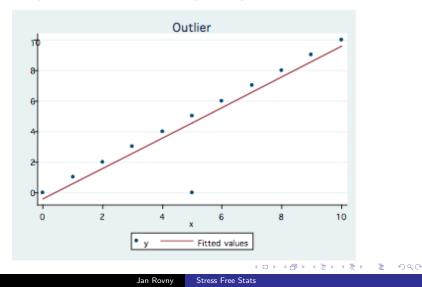
Figure: Perfect Line

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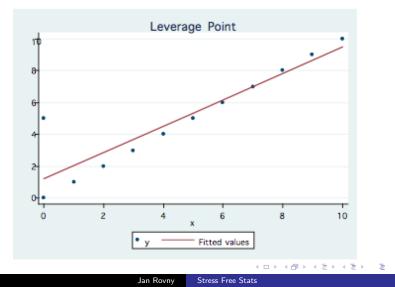
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Outlier is a point with a large residual. An outlier does not influence the slope of the regression, but it effects the intercept (it will affect the value of y when the regression line passes through the origin). Remember that: $u_i = (Y_i - \hat{Y})$



Leverage point is disproportionately distant from the bulk of the values of the predictor(s). Is capable of pulling the regression line towards itself, thus distorting the slope. In such a case, it is an influential data point.



Influential point is both an outlier and a leverage point. It modifies both the slope and the intercept of your regression line and may completely drive all the results.

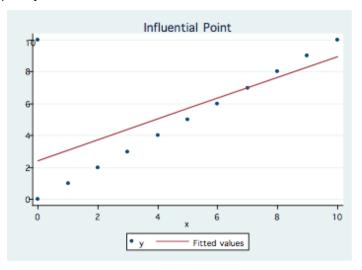


Figure: Influential Point < => < => < => < => > = <

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DFITS

- Tells us the influence of an observation on predicted values (regression line)
- It runs regressions with and without each observation
- A highly influential observation is one where $|DFITS| > 2\sqrt{\frac{k}{N}}$
- R:
 - dffits(modelname) # creates observations of influence
 - large<-dffits(modelname)>2*sqrt(k/n) # creates object
 - list(large)
- This will tell you which particular observations are influencing your results

DFBETAs

- $\bullet\,$ Tells us the influence of an observation on each β coefficient
- A highly influential observation is one where $|DFBETA| > 2/\sqrt{n}$
- R
- dfbetasPlots(model) # produces a plot for each coefficient (car library)
- dfbetas(model) # creates observations of influence on each coefficient
- DF<-abs(dfbetas(model) # assign abs. dfbetas to matrix DF
- list(DF>2/sqrt(n)) # identify influential observations on all coeffs.
- This well tell you which particular observations are influencing β_1

- The RULE is not to select on your dependent variable, so throwing the influential point out is not a solution!
 - If the observation belongs to the target population and there is no coding error, throwing out the point carries worse problems with the estimation.
 - Present the original results as main results and in the appendix show the results with the influential point removed, showing the influence of the point in your results.
 - Find other estimator better than OLS, an alternative fit measure (paying the cost of being less efficient than OLS) – this is a matter for another class.